

11/17 Aim: Practice Constructions

Get out your construction supplies.

Homework:  
Quest Wednesday

Nov 5-6:19 AM

[mathopenref.com](http://mathopenref.com)

this is a great website for constructions and other topics

Nov 6-6:27 AM

Vocabulary:  
median of a triangle

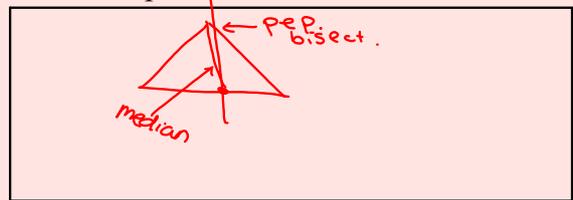
is a line segment that goes from a vertex of the triangle to the midpoint of the opposite side.



Nov 5-6:22 AM

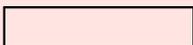
How do you construct a median of a triangle?

A median is drawn by constructing a perpendicular bisector of a side of the triangle locating the midpoint and then drawing a segment from a vertex to the midpoint.



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The CENTROID is the point where the three medians of the triangle intersect.



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The Centroid divides the median into two parts in a 2:1 ratio

OM = 2  
CO = 4  
MC = 6

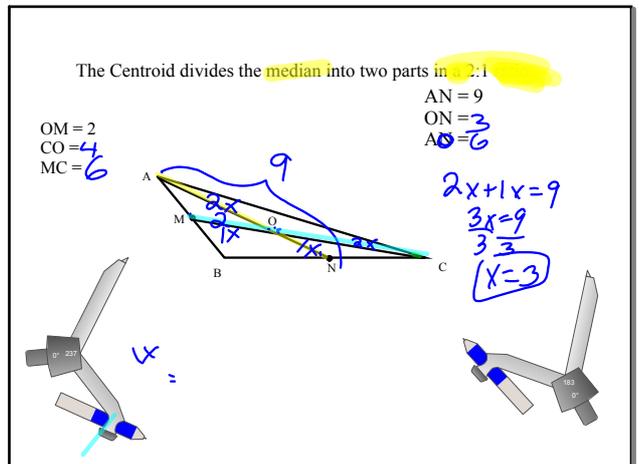
AN = 9  
ON = 3  
AO = 6

$$2x + x = 9$$

$$3x = 9$$

$$\frac{3x}{3} = \frac{9}{3}$$

$$x = 3$$



Nov 14-1:51 PM

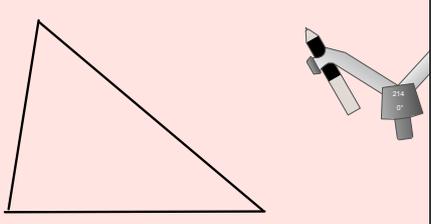
<http://www.mathopenref.com/trianglecentroid.html>

Nov 6-6:53 AM

The **centroid** has one **very special** feature it is known as the center of gravity of the triangle.

Nov 5-6:49 AM

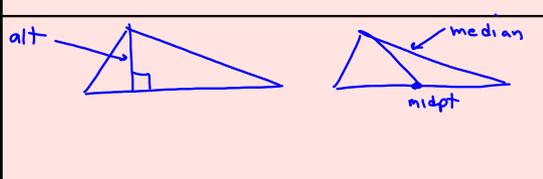
Construct the median of two sides  
Locate the centroid.



Nov 5-6:34 AM

Vocabulary:  
Altitude of a triangle

is a line segment that goes from a vertex perpendicular to the opposite side of a triangle.



Nov 5-6:24 AM

How do you construct an altitude of a triangle?

Construct a perpendicular line from a point not on the line.

Nov 5-6:25 AM

The **orthocenter** is the point where the three **altitudes** of the triangle intersect.

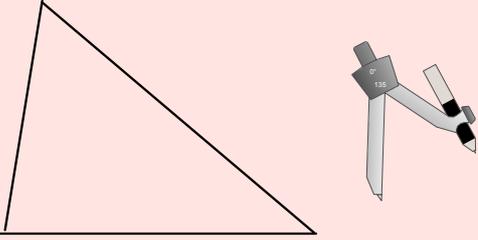
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<http://www.mathopenref.com/triangleorthocenter.html>

What is a special feature that happens in an orthocenter?  
Watch closely.

Nov 5-7:07 AM

Draw a scalene triangle  
construct two altitudes for the triangle



Nov 5-6:40 AM

Vocabulary:  
Angle bisector

is a segment that divides an angle into two congruent angles



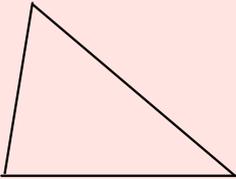
Nov 6-6:56 AM

The incenter is the point where the three angle bisectors of the triangle intersect.



Nov 5-6:28 AM

Draw a scalene triangle  
construct three angle bisectors for the triangle

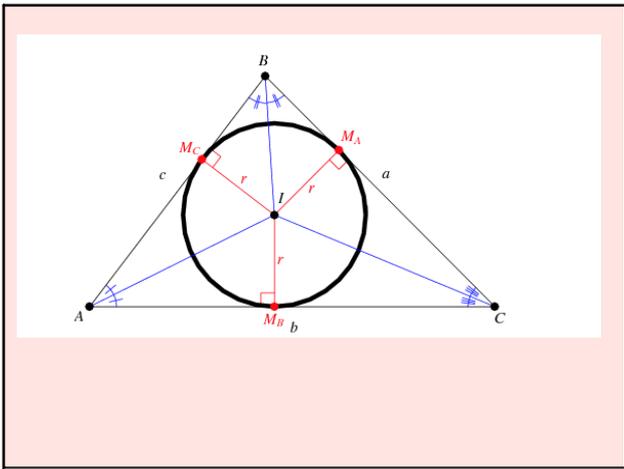


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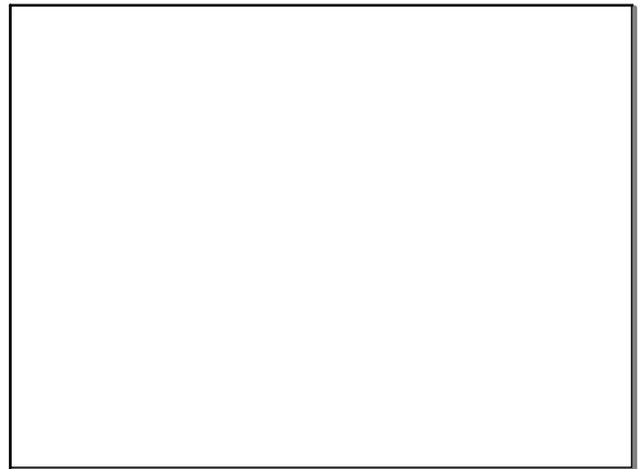
The incenter is the center of the triangle's incircle, the largest circle that will fit inside the triangle and touch all three sides.

<http://www.mathopenref.com/triangleincenter.html>

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Nov 6-7:41 AM



Nov 22-10:41 AM

Can the point of intersection every fall outside of the triangle?  
Under what circumstances would this happen?

The Circumcenter is the point where the three **perpendicular bisectors** of the triangle intersect.

the circle that passes through all three of the triangle's vertices. As you reshape the triangle above, notice that the circumcenter may lie outside the triangle.

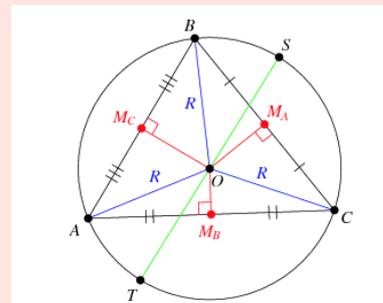


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<http://www.mathopenref.com/trianglecircumcenter.html>

The circumcenter is also the center of the triangle's **circumcircle** - the circle that passes through all three of the triangle's **vertices**.



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Nov 6-7:42 AM

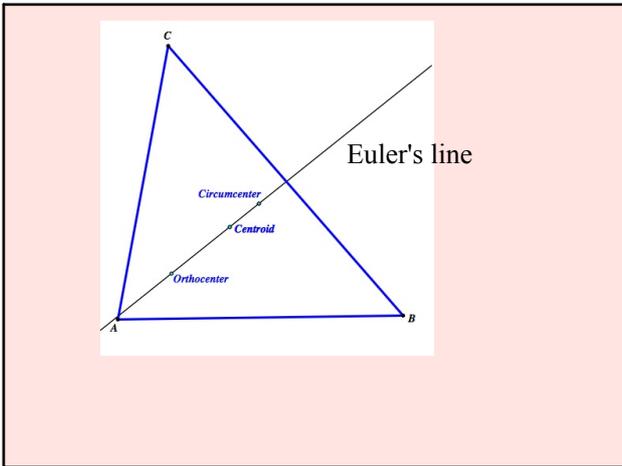
In the case of an equilateral triangle, *all four* of the above centers occur at the same point.

### The Euler line - an interesting fact

It turns out that the orthocenter, centroid, and circumcenter of any triangle are collinear - that is, they always lie on the same straight line called the Euler line, named after its discoverer.

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Nov 5-7:10 AM



- 1) In what type of triangle is the point of concurrency inside a triangle the same for the incenter, circumcenter, orthocenter, and centroid?
  - 1) obtuse
  - 2) isosceles
  - 3) equilateral
  - 4) scalene
- 2) What point of concurrency in a right triangle is also the midpoint of the hypotenuse?
  - 1) circumcenter
  - 2) centroid
  - 3) incenter
  - 4) orthocenter
- 3) The circumcenter of a triangle is also the center of
  - 1) mass and balance
  - 2) a circle circumscribing the triangle
  - 3) a circle inscribed inside the triangle
  - 4) all of the above
- 4) The incenter of a triangle is also the center of
  - 1) mass and balance
  - 2) a circle circumscribing the triangle
  - 3) a circle inscribed inside the triangle
  - 4) all of the above

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- 5) What point of concurrency in a triangle divides the medians into segments whose measures are in the ratio of 2:1?
  - 1) orthocenter
  - 2) centroid
  - 3) incenter
  - 4) circumcenter
- 6) What point of concurrency in a triangle is *always* located inside the triangle?
  - 1) orthocenter and circumcenter
  - 2) incenter, only
  - 3) orthocenter, only
  - 4) centroid and incenter
- 7) The centroid of a triangle is also the center of
  - 1) mass and balance
  - 2) a circle circumscribing the triangle
  - 3) a circle inscribed inside the triangle
  - 4) all of the above
- 8) In what type of triangle is the orthocenter located outside of the triangle?
  - 1) equilateral
  - 2) obtuse
  - 3) acute
  - 4) right

- 1) The centroid of a triangle is the point of concurrency of what lines of a triangle?
  - 1) bisectors of the angles
  - 2) altitudes
  - 3) perpendicular bisectors of the sides
  - 4) medians
- 2) The circumcenter of a triangle is the point of concurrency of what lines of a triangle?
  - 1) medians
  - 2) perpendicular bisectors of the sides
  - 3) altitudes
  - 4) bisectors of the angles
- 3) The incenter of a triangle is the point of concurrency of what lines of a triangle?
  - 1) medians
  - 2) perpendicular bisectors of the sides
  - 3) bisectors of the angles
  - 4) altitudes
- 4) The orthocenter of a triangle is the point of concurrency of what lines of a triangle?
  - 1) medians
  - 2) perpendicular bisectors of the sides
  - 3) altitudes
  - 4) bisectors of the angles

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5) The midpoint of the hypotenuse of a right triangle is also the

1) orthocenter	3) incenter
2) circumcenter	4) centroid

6) It is possible for which of the following points to lie in the exterior region of a triangle?

1) circumcenter and centroid, only	3) orthocenter, only
2) circumcenter, only	4) orthocenter and circumcenter, only

7) The circumcenter of a triangle is also the center of

1) mass and balance	3) a circle inscribed inside the triangle
2) a circle circumscribing the triangle	4) all of the above

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8) The incenter of a triangle is also the center of

1) mass and balance	3) a circle inscribed inside the triangle
2) a circle circumscribing the triangle	4) all of the above

9) What point of concurrency in a triangle divides the medians into segments whose measures are in the ratio of 2:

1) orthocenter	2) centroid	3) incenter	4) circumcenter
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10) The centroid of a triangle is also the center of

1) mass and balance	3) a circle inscribed inside the triangle
2) a circle circumscribing the triangle	4) all of the above

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